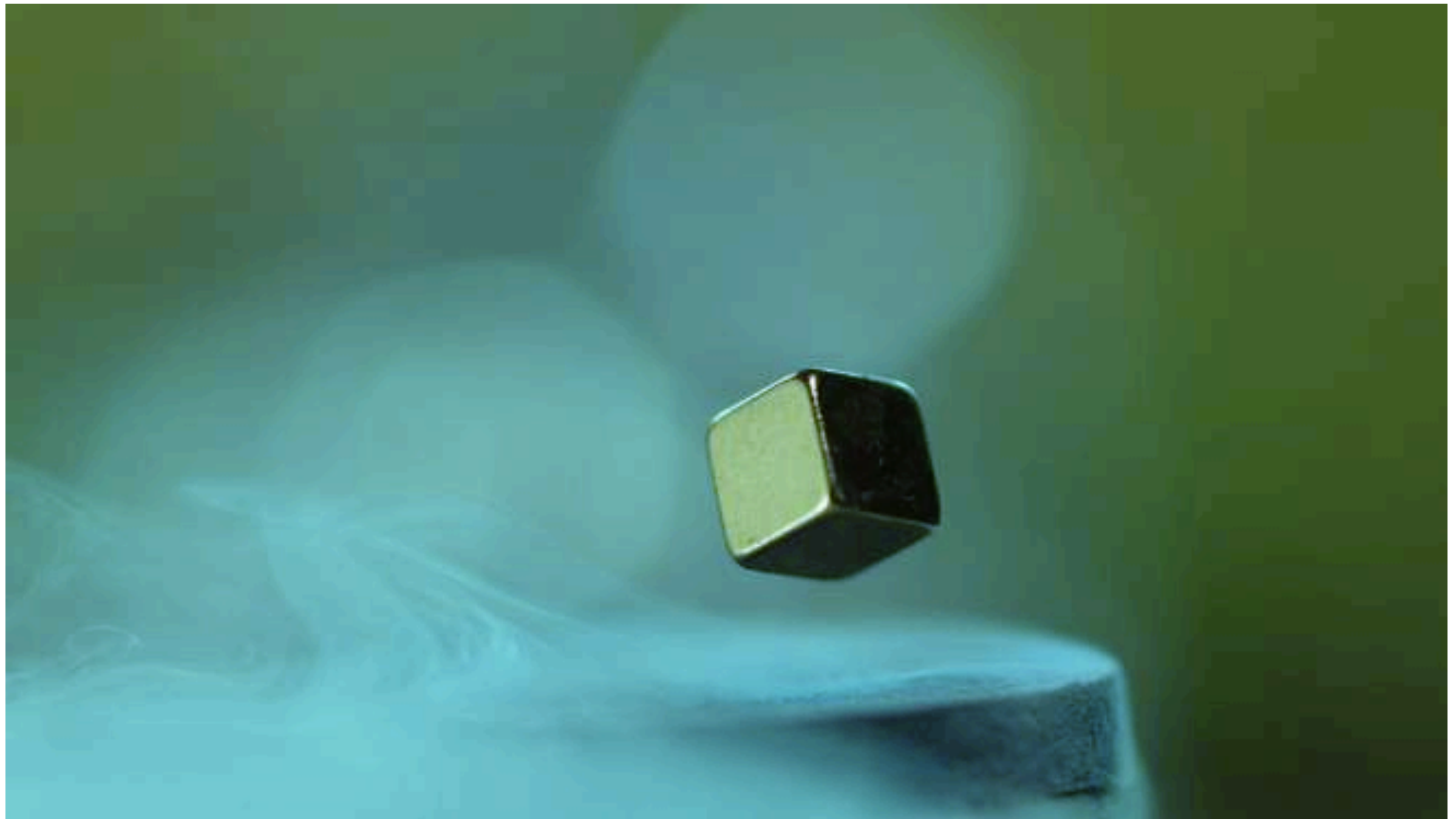


# Aspects of Superconductivity



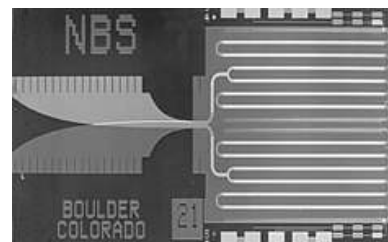
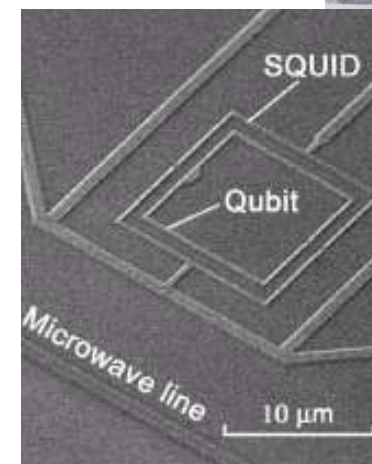
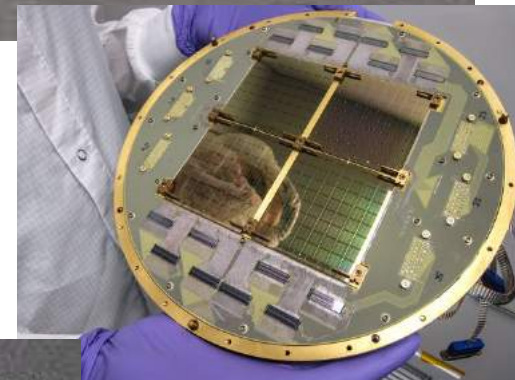
**Aline Ramires**  
**ETH Zurich → ICTP-SAIFR ↔ MPI-PKS**

# Applications?

- Low loss power transmission lines
- Turbines and generators
- Maglev trains
- Magnetic resonance imaging (MRI)
- Tokamaks (for nuclear fusion)
- Bolometers (for particle detection in astronomy and cosmology)
- Particle accelerators/LHC (as beam-steering and focusing magnets)
- The basis of the most sensitive magnetometers (SQUIDs)
- The basis of Q-bits for quantum computation
- The basis of the VOLT standard
- ...

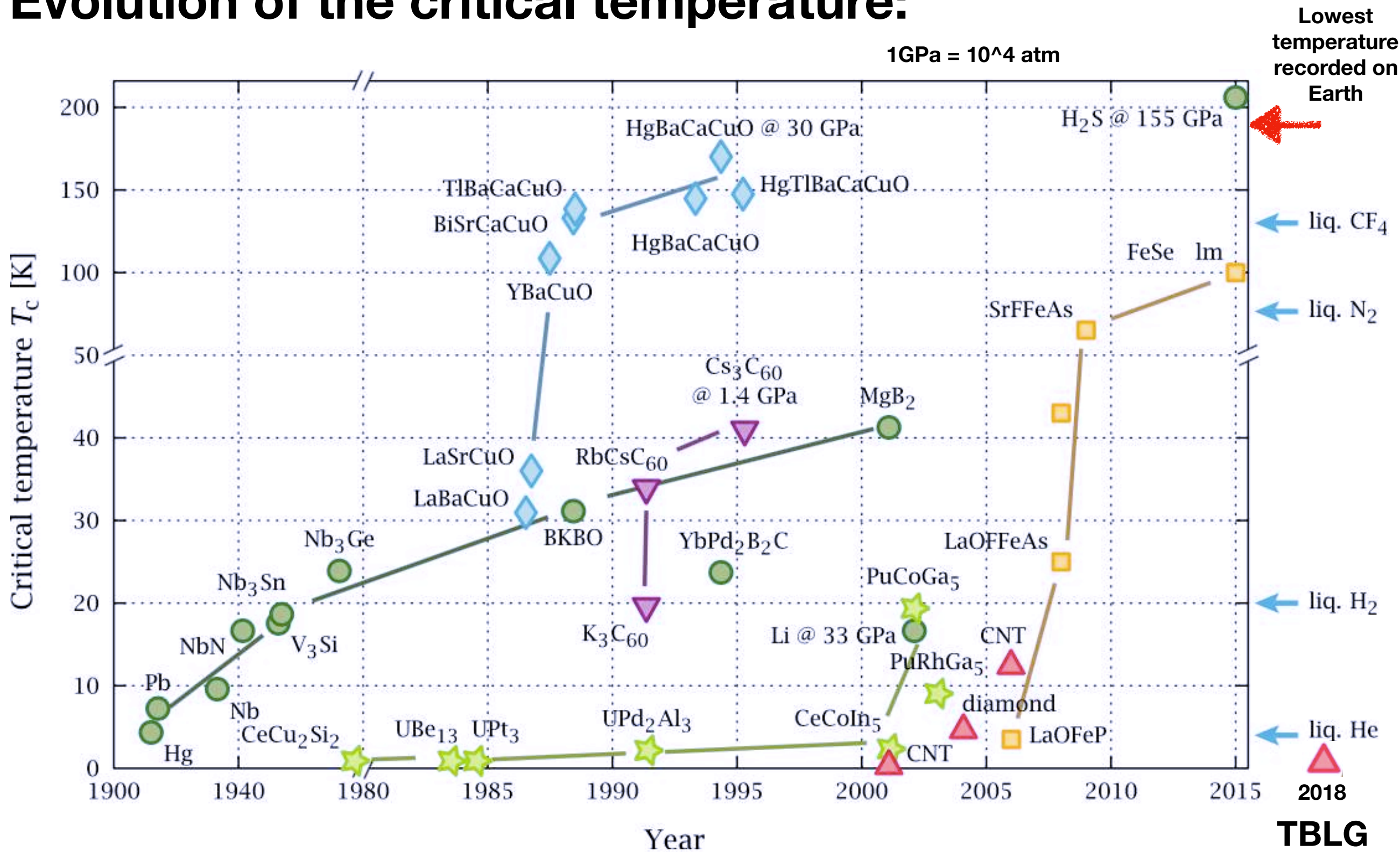
**Great impact on numerous areas:**

- Power production/storage/distribution
- Transport
- Medicine
- Scientific instrumentation
- New quantum technologies
- ...



**Main current limitation: SC only at very low temperatures!**

# Evolution of the critical temperature:





# Evolution of the critical temperature:

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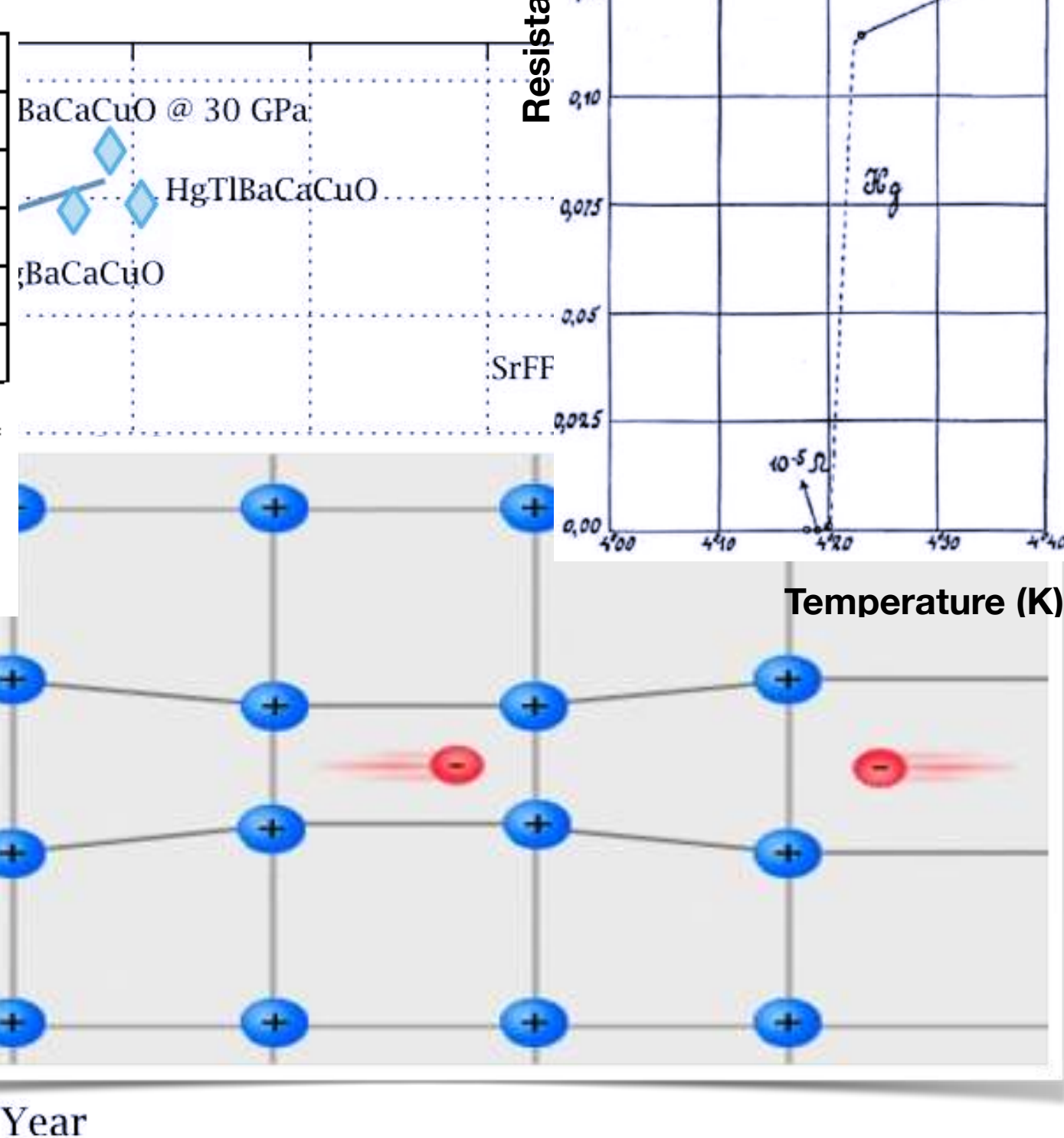
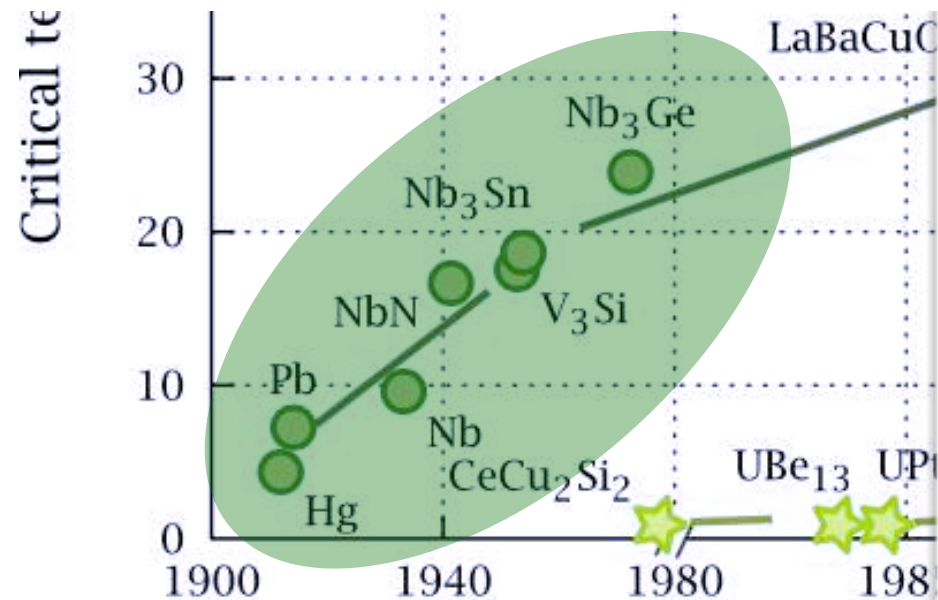
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\* Lanthanide Series  
+ Actinide Series

58	59	60	61	62	63	64	65	66	67	68	69	70	71
Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu
90	91	92	93	94	95	96	97	98	99	100	101	102	103
Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr



## Elemental Materials and Alloys

- Conventional Superconductivity
- Well described by BCS theory. Phonon mediated.

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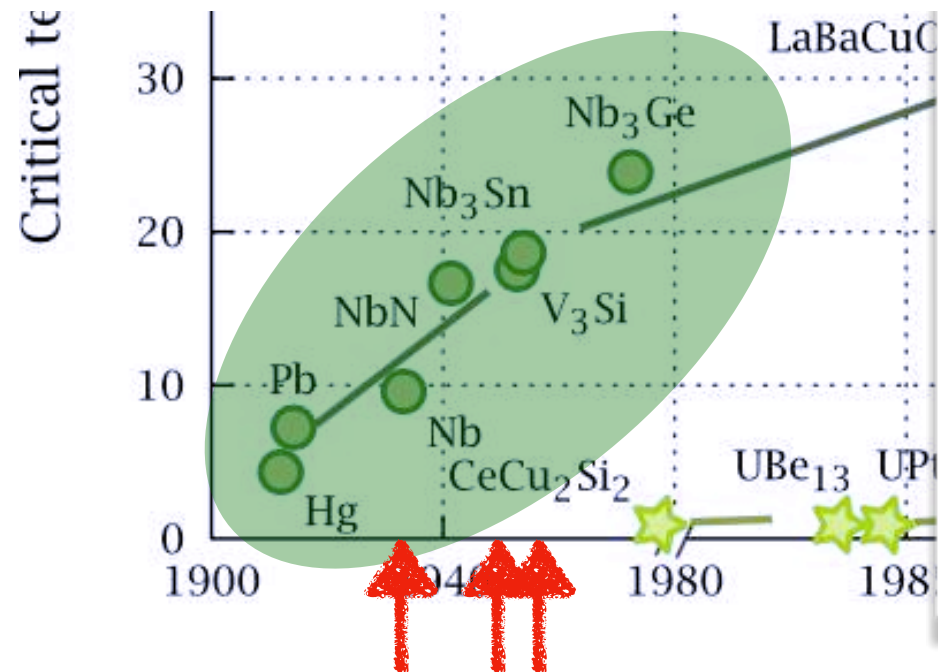
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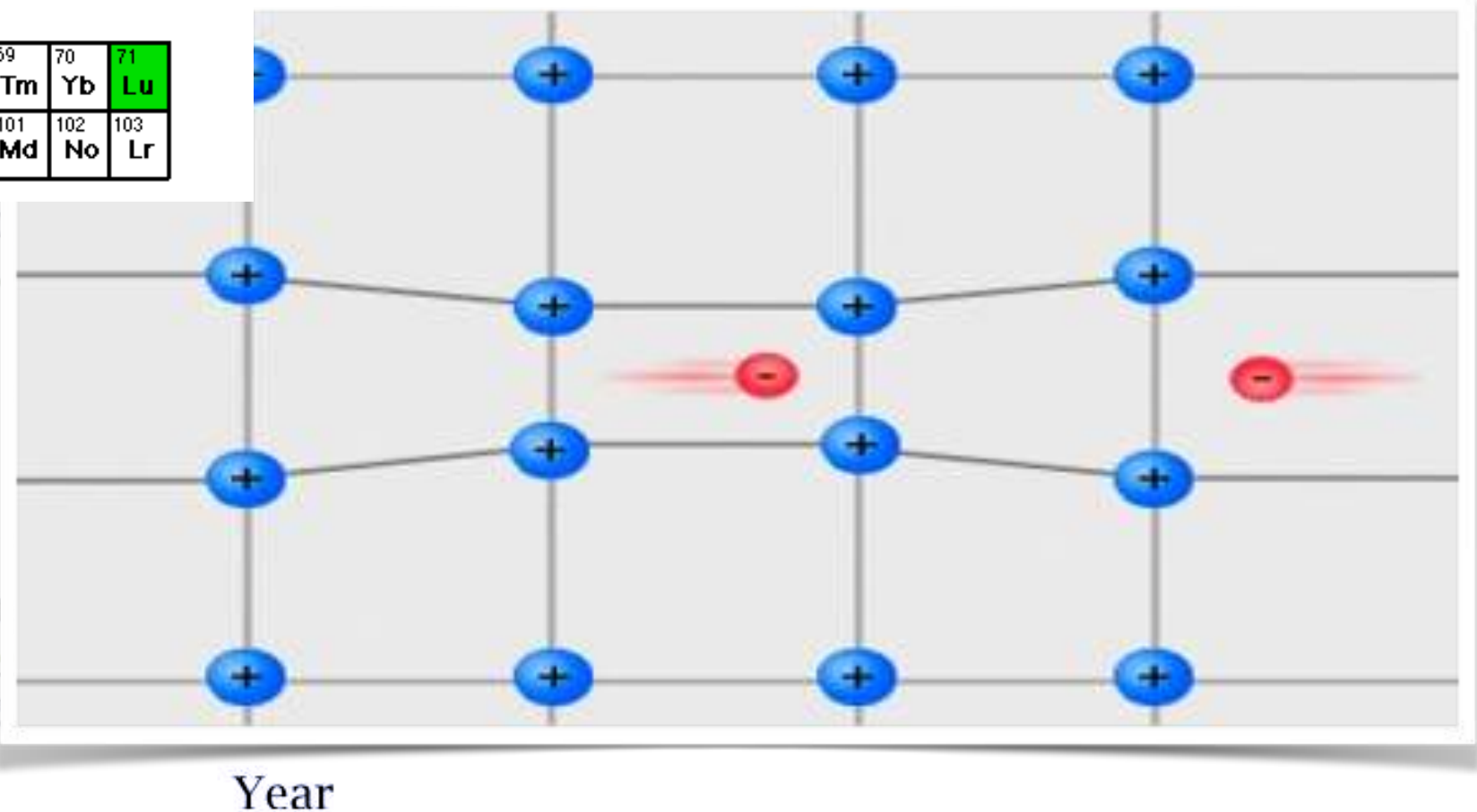
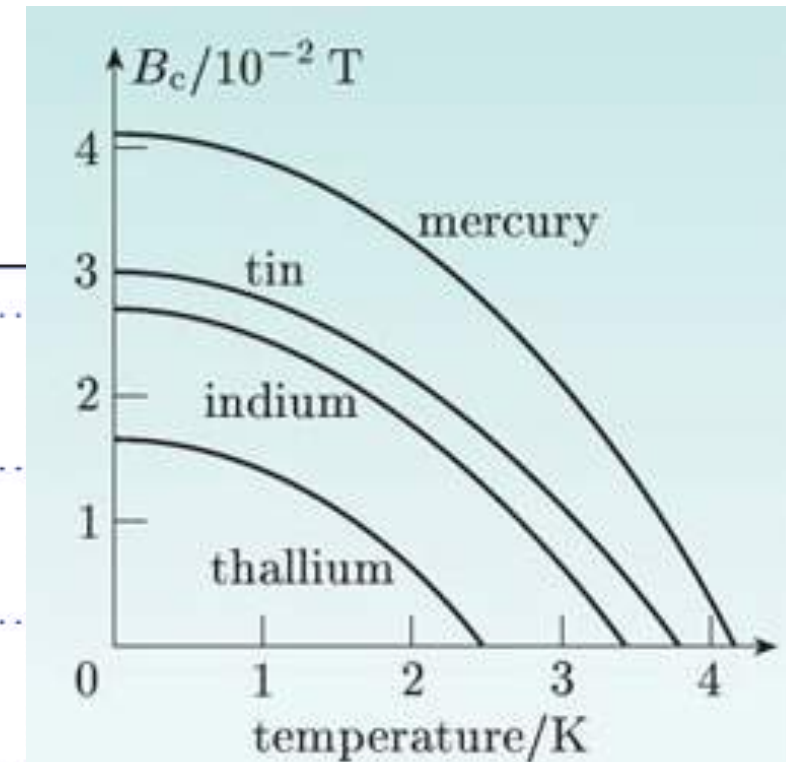
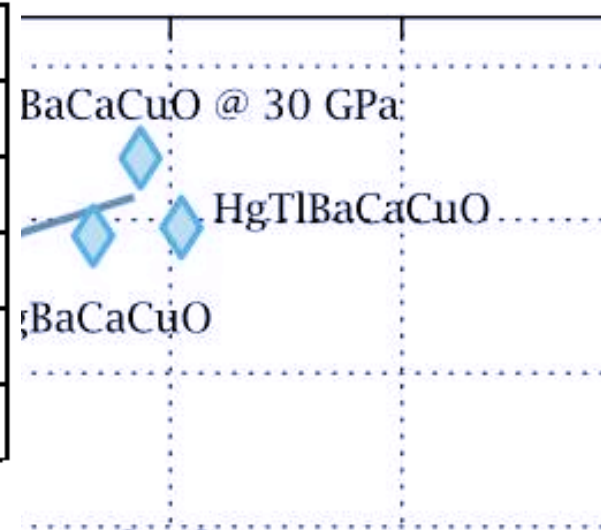
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\* Lanthanide Series  
+ Actinide Series

58	59	60	61	62	63	64	65	66	67	68	69	70	71
Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu
90	91	92	93	94	95	96	97	98	99	100	101	102	103
Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr

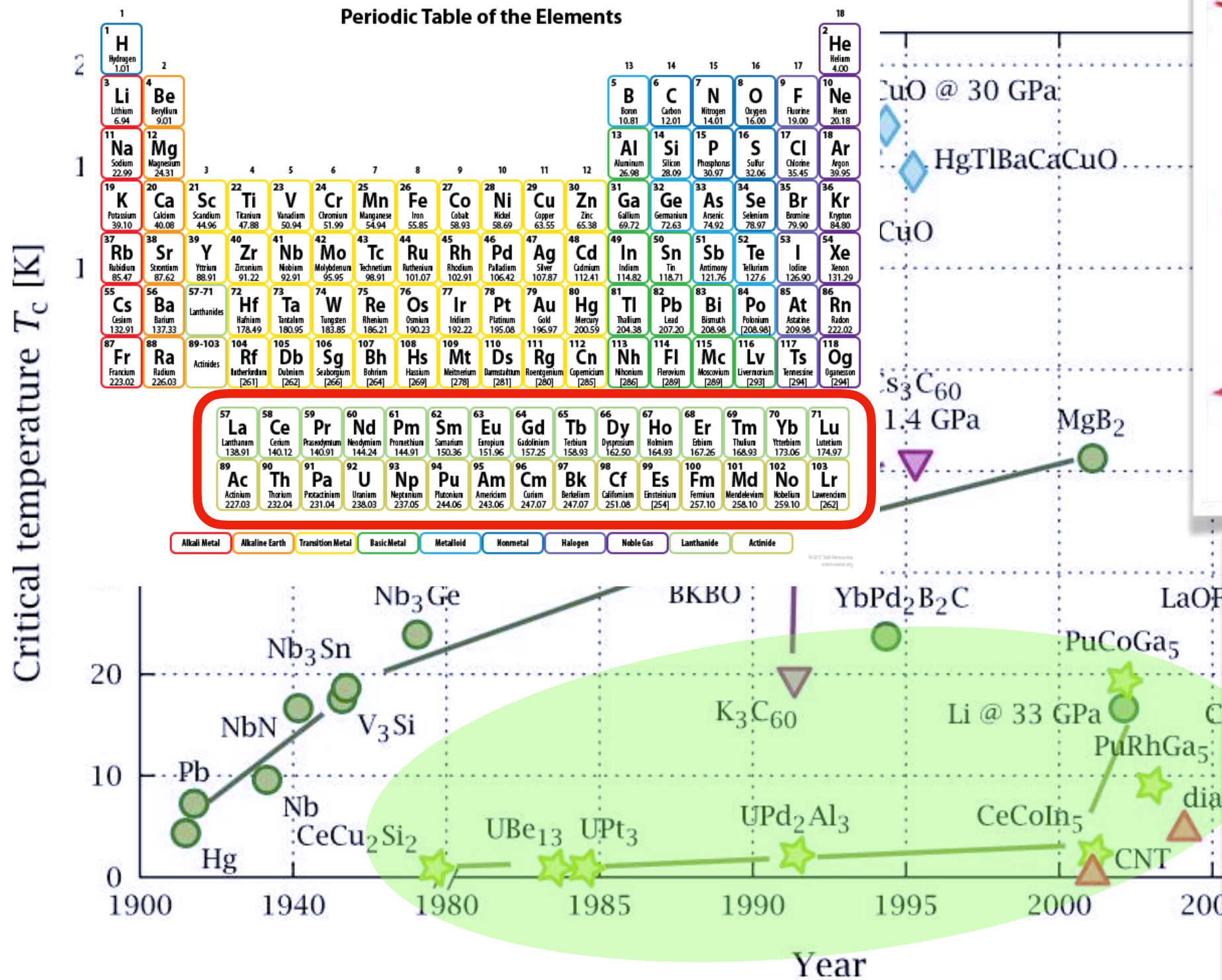


**1935: London Theory**  
**1950: Ginzburg-Landau Theory**  
**1957: BCS Theory**



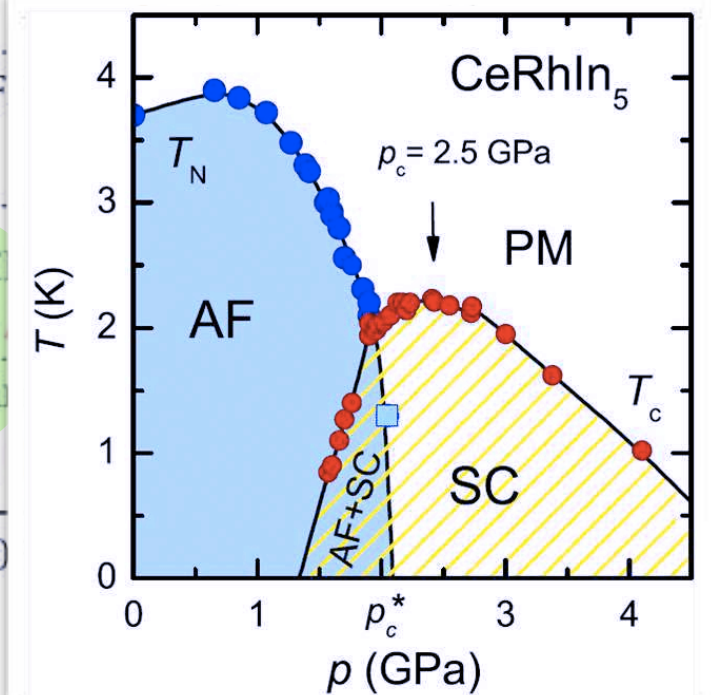
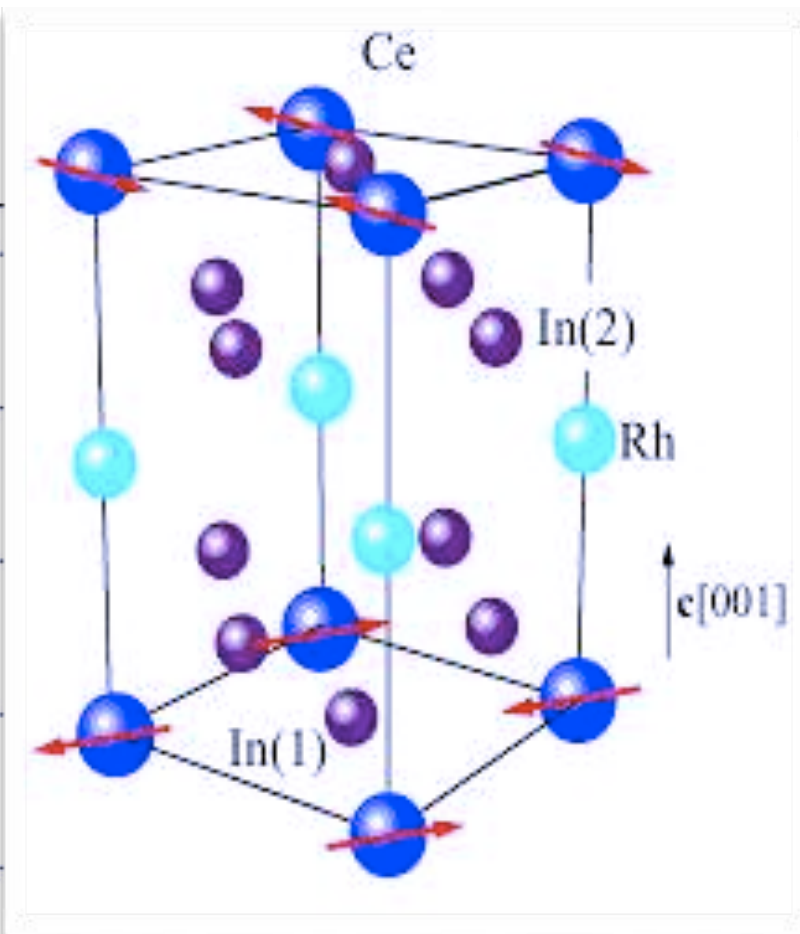


# Evolution of the critical temperature:



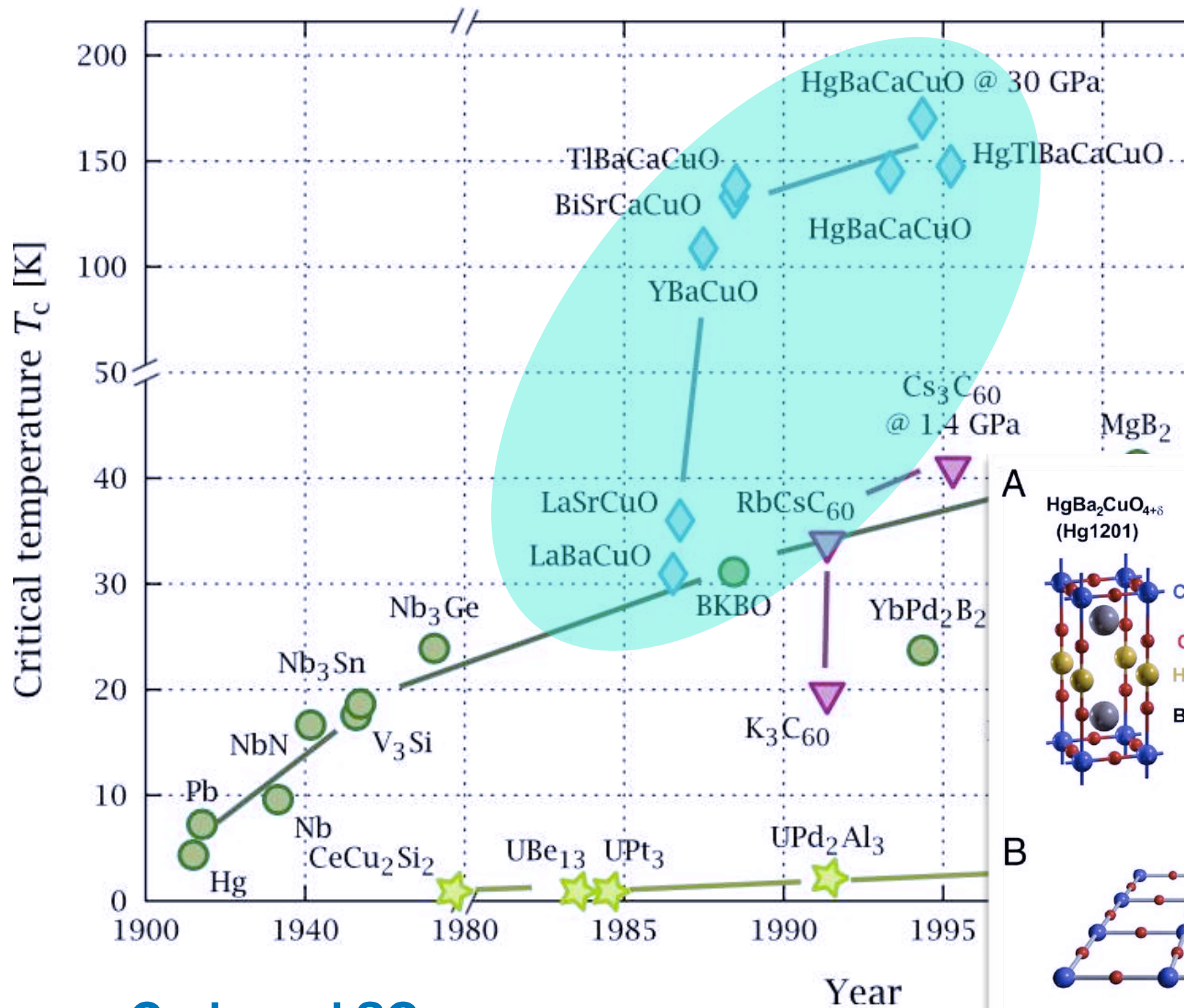
## Heavy Fermions

- Strong correlations. Unconventional SC. Non-phonon mediated.
- Neighbouring magnetism?



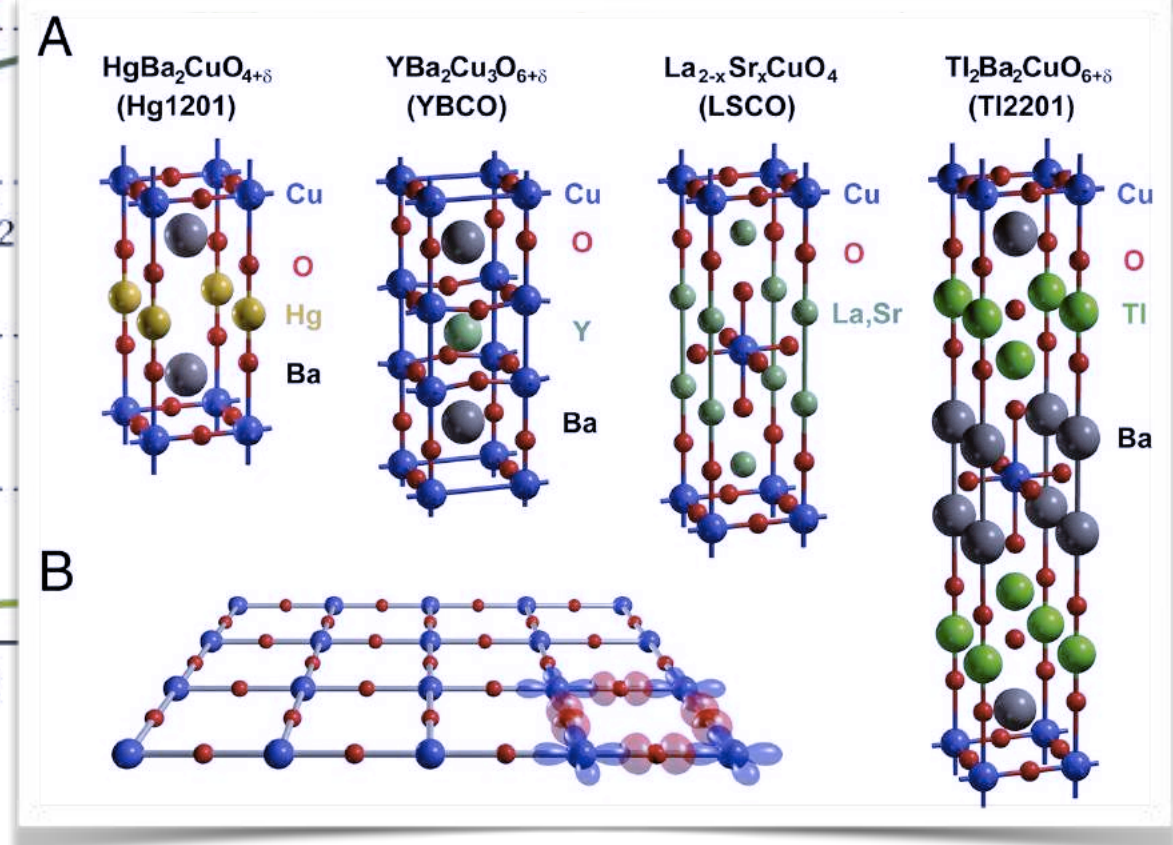
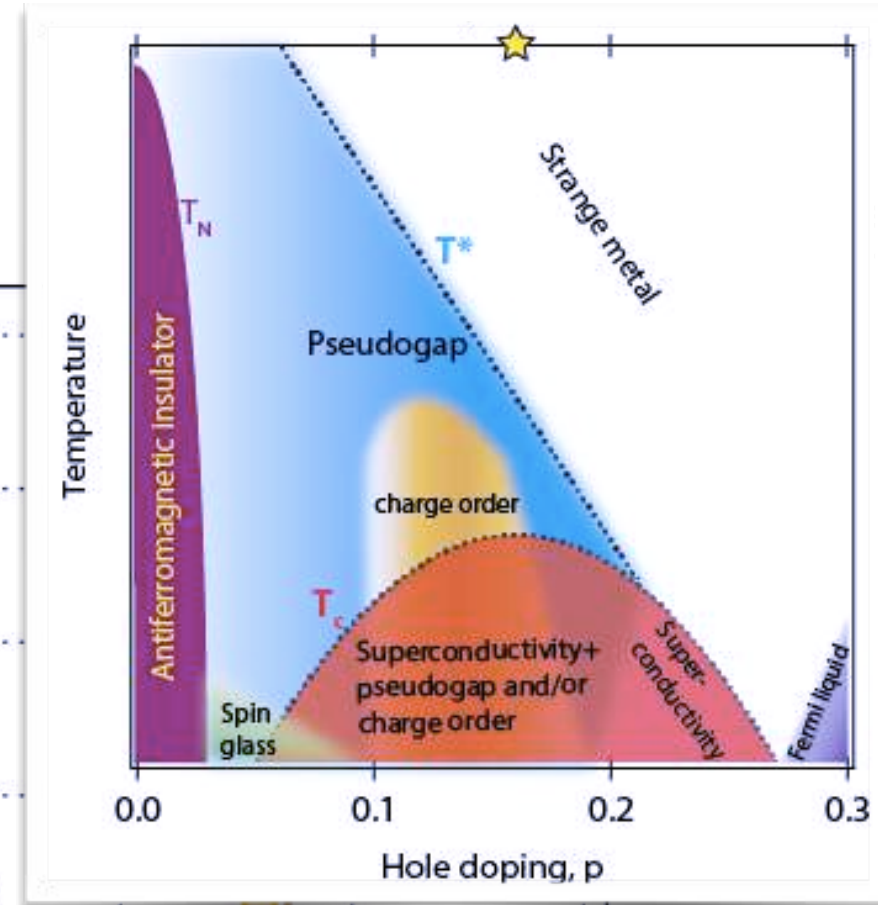


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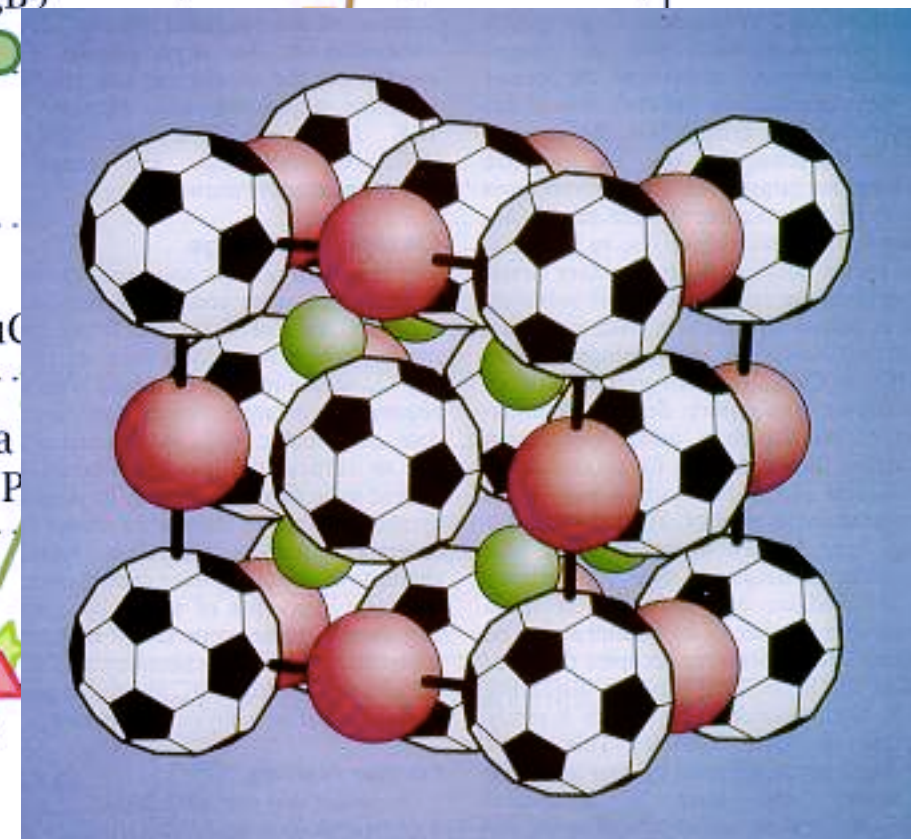
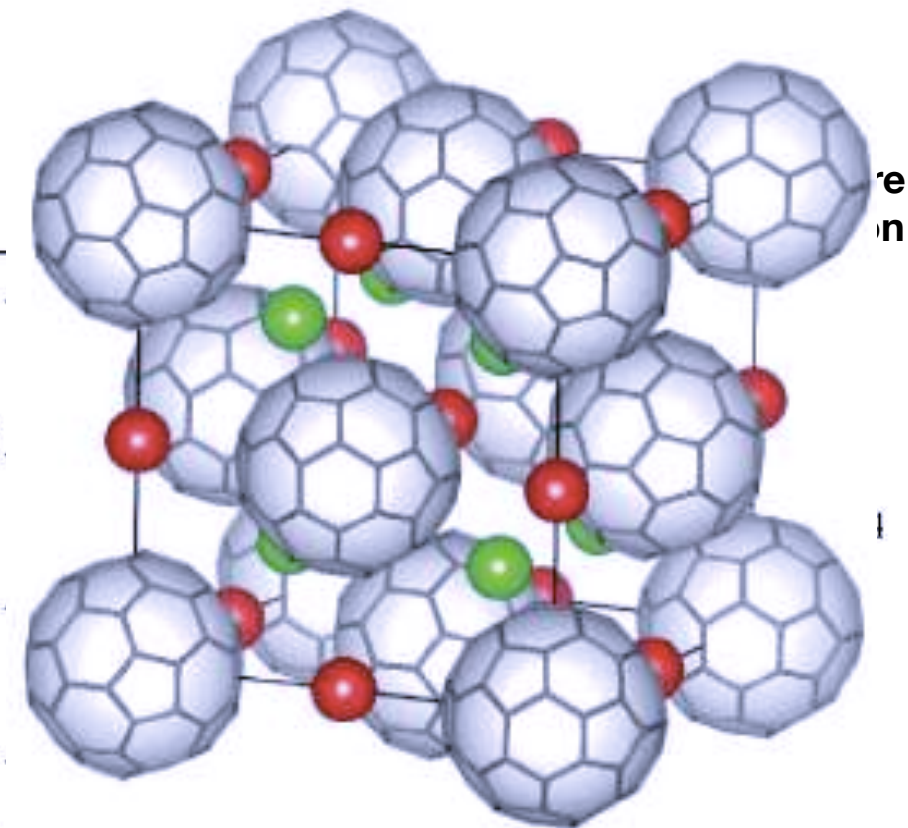
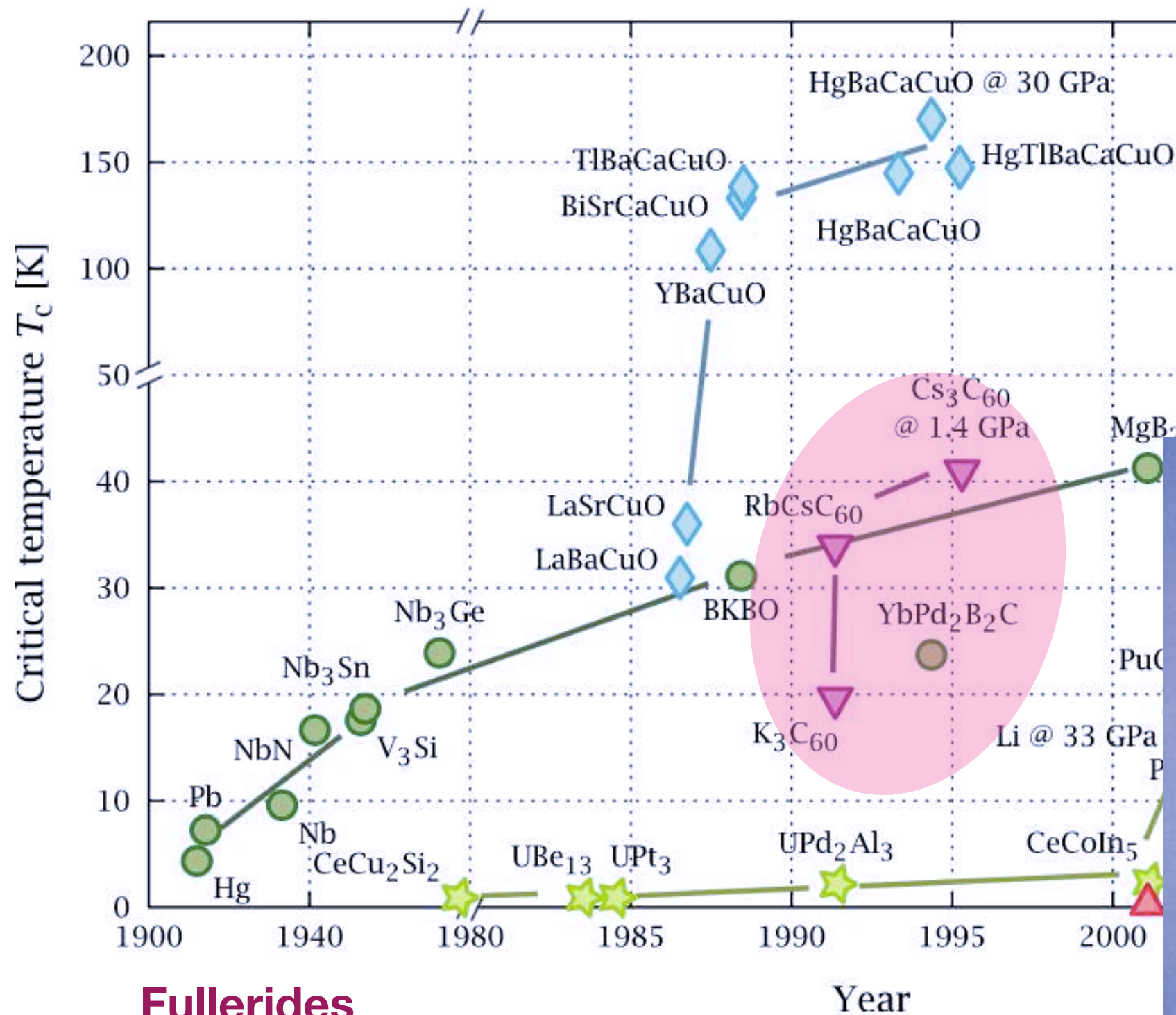
## Cu-based SC

- Complex phase diagram. Unconventional SC. Non-phonon mediated.





# Evolution of the critical temperature:

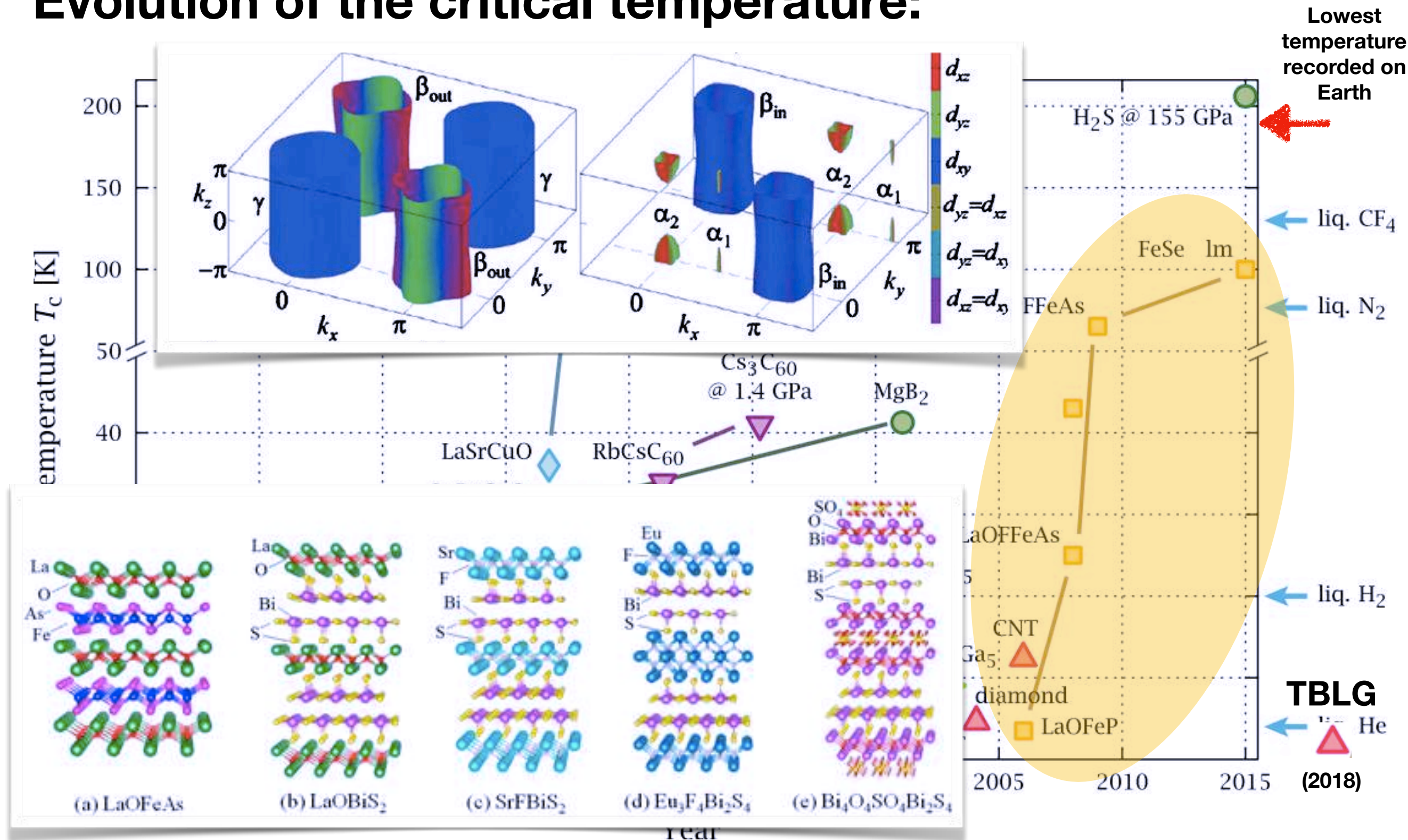


## Fullerides

- SC in organic/molecular solids
- Very sensitive materials. Conventional superconductors



# Evolution of the critical temperature:



Fe-based SC

- Many orbitals and Fermi surfaces contribute to SC

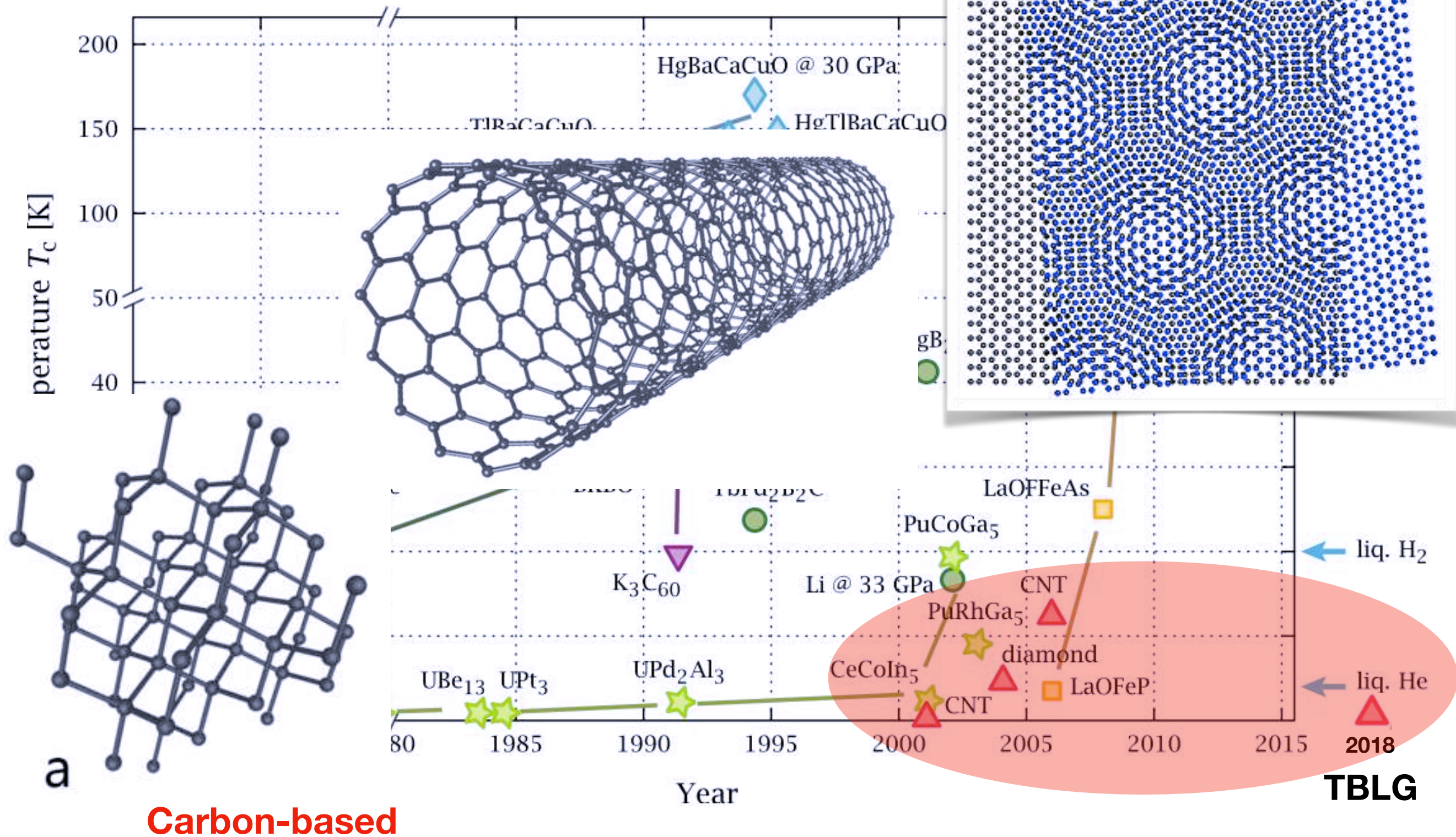
Image credit: Wikipedia (By PJRay - Own work, CC BY-SA 4.0)

Y. Mizuguchi, Condens. Matte. (2017)

Y. Wang, PRB (2013)

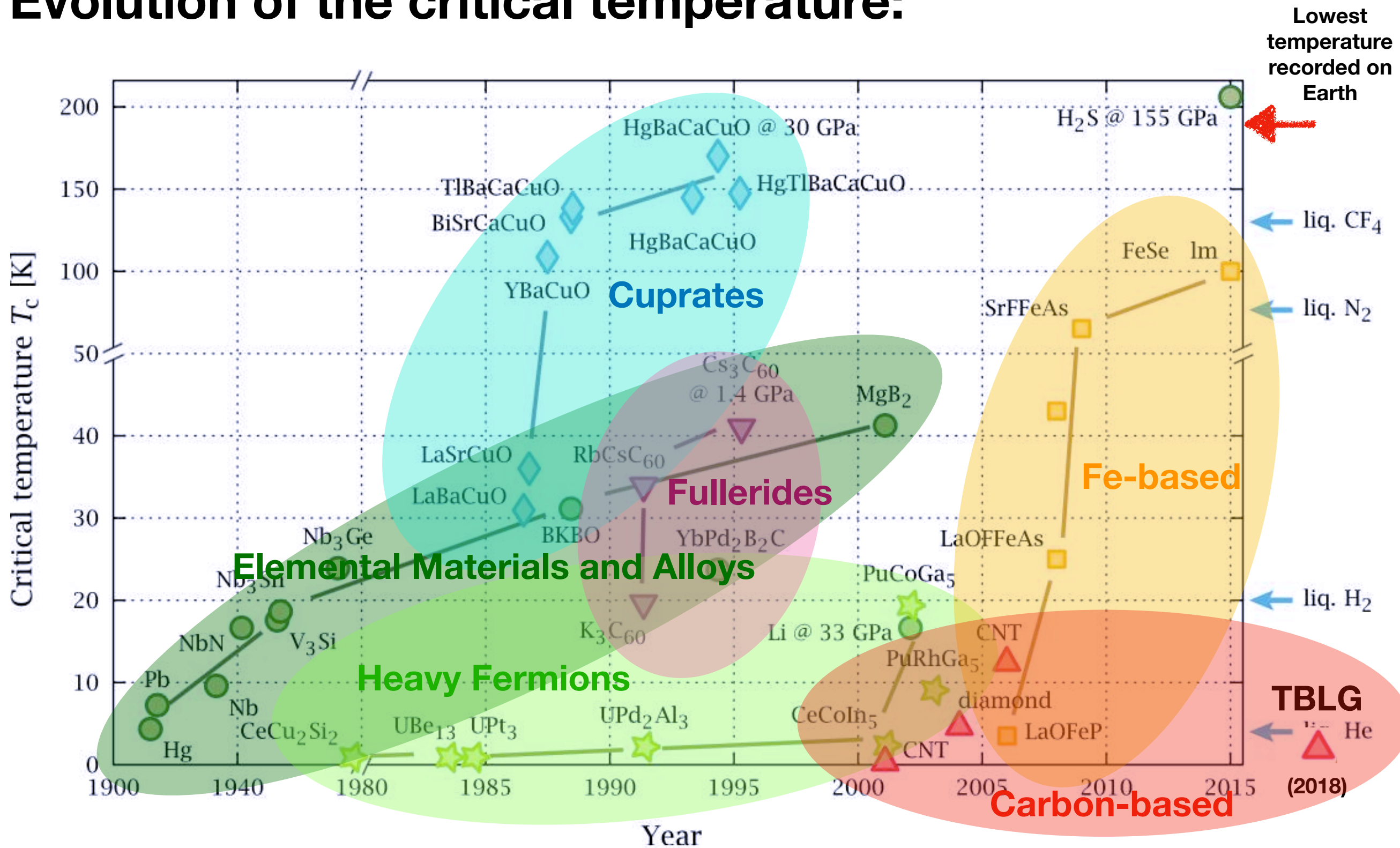


# Evolution of the critical temperature:





# Evolution of the critical temperature:



**SC was not predicted: it was discovered.**



# Some more historical remarks:

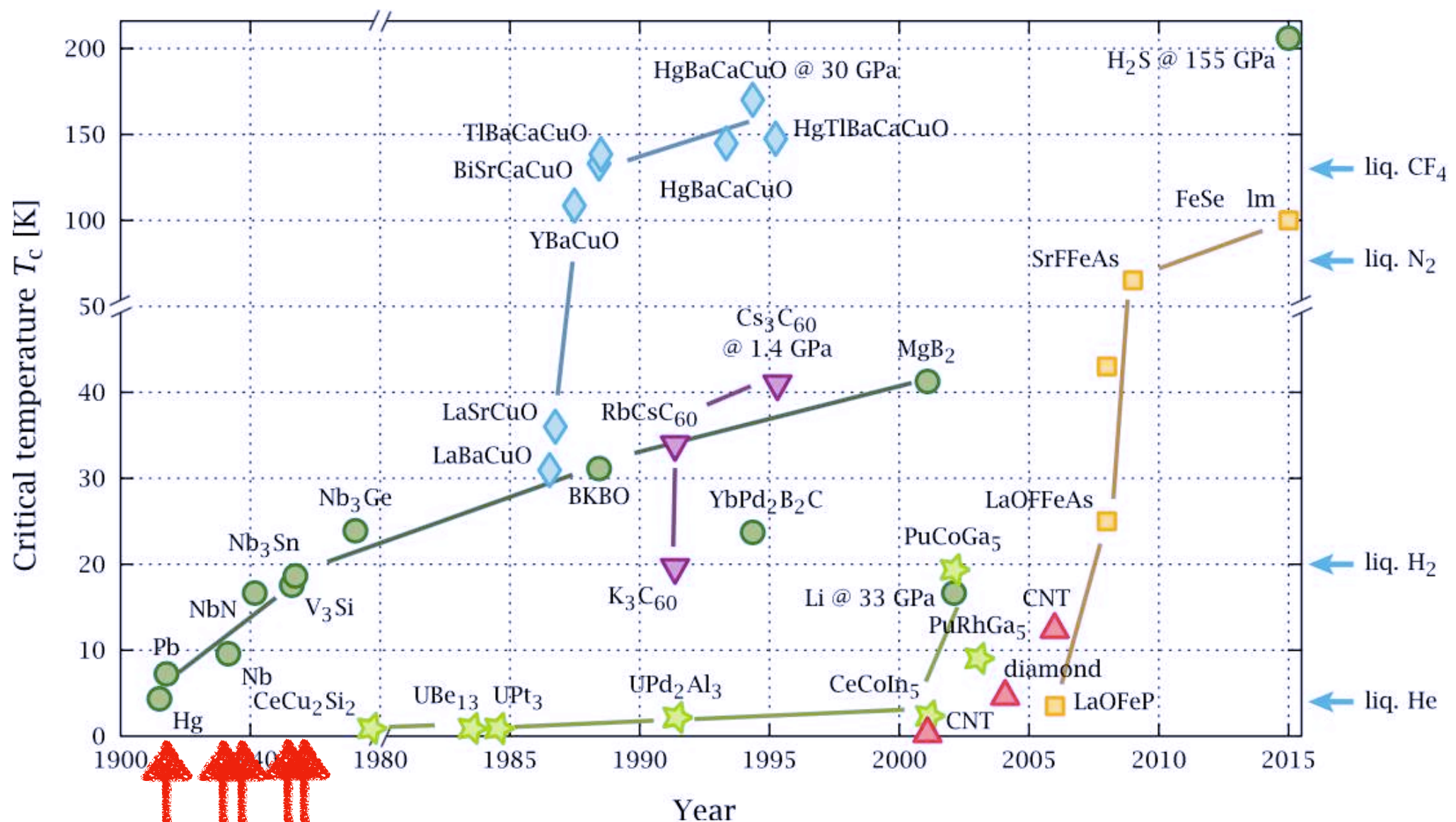
1911: Kamerlingh Onnes observed **zero resistance** of Hg below 4K

1933: Meissner and Ochsenfeld observed the phenomena of **flux expulsion**

1935: London Theory (Phenomenological)

1950: Ginzburg-Landau Theory (Phenomenological)

1957: BCS Theory (Microscopic)



46 years

Still some debate on the microscopic mechanism  
for pairing for unconventional SC

# Failed theories of superconductivity

Jörg Schmalian

Department of Physics and Astronomy, and Ames Laboratory, Iowa State  
University, Ames, IA 50011, USA

**Almost half a century passed between the discovery of superconductivity by Kamerlingh Onnes and the theoretical explanation of the phenomenon by Bardeen, Cooper and Schrieffer. During the intervening years the brightest minds in theoretical physics tried and failed to develop a microscopic understanding of the effect. A summary of some of those unsuccessful attempts to understand superconductivity not only demonstrates the extraordinary achievement made by formulating the BCS theory, but also illustrates that mistakes are a natural and healthy part of the scientific discourse, and that inapplicable, even incorrect theories can turn out to be interesting and inspiring.**



[https://www.youtube.com/watch?v=2pB87H3\\_F\\_c&t=2s](https://www.youtube.com/watch?v=2pB87H3_F_c&t=2s)

<https://www.youtube.com/watch?v=PqSgmCg1kew&t=1s>



# Outline

**What are superconductors?**

**What are their defining properties?**

**Are superconductors simply perfect conductors?**

**London Theory**

**Landau Theory**

**Ginzburg-Landau Theory**

**Ginzburg-Landau Theory**

**Flux Quantization\Recover London Theory**

**Josephson Junction**

**SQUIDS**

**Back to the start...**

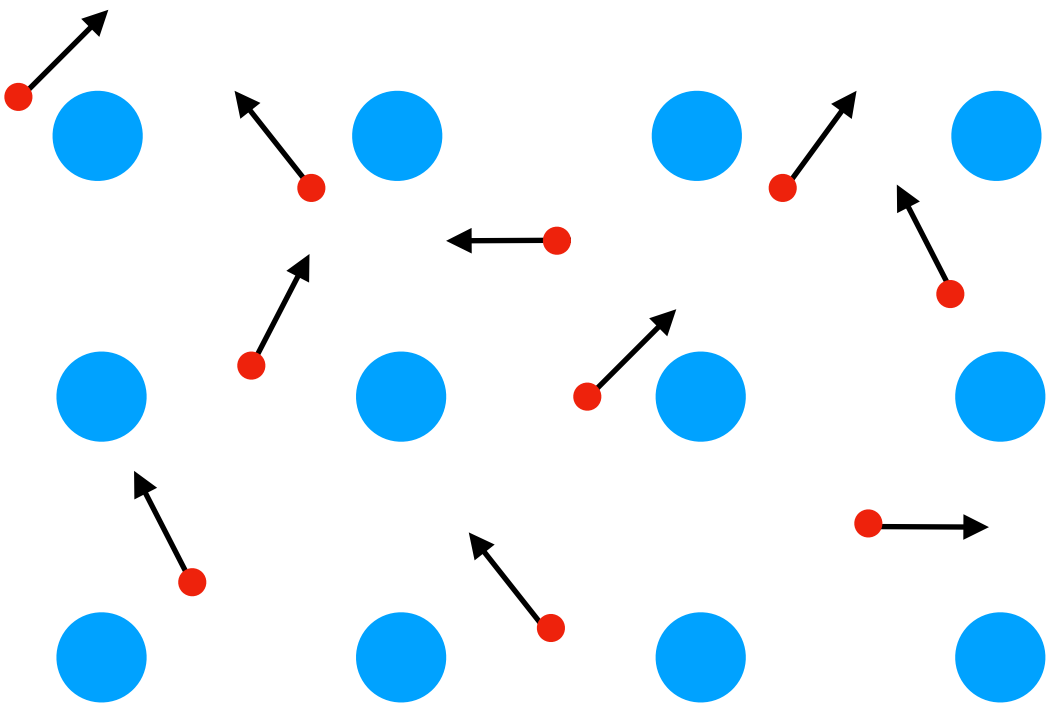




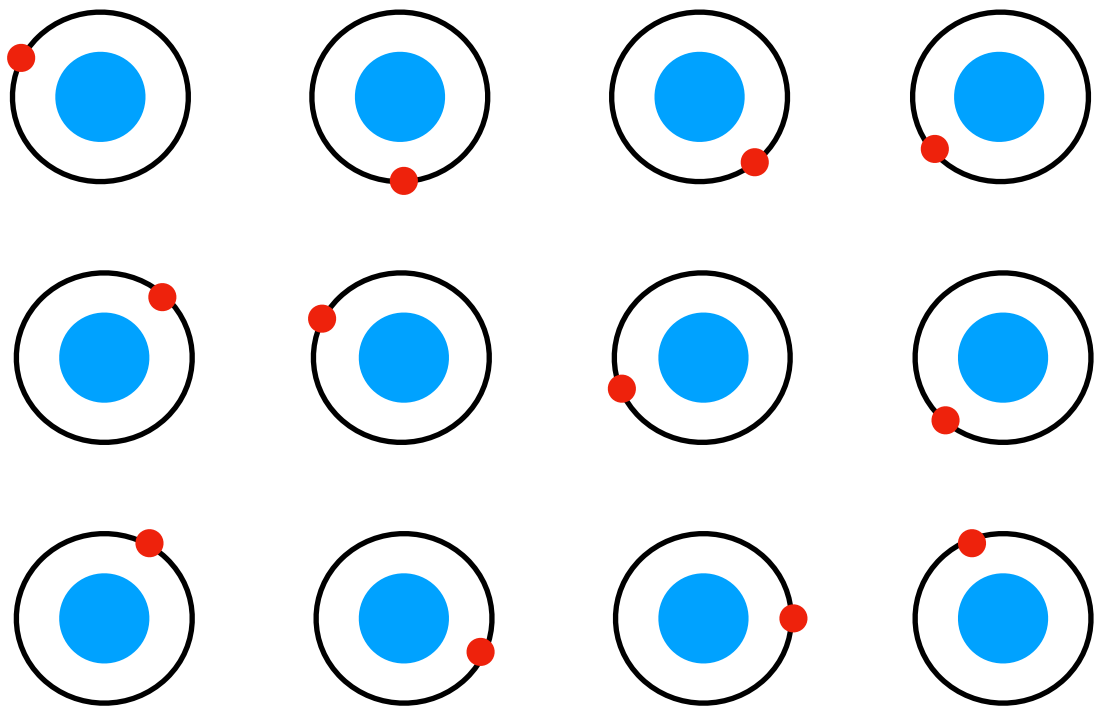
# How do metals behave at low T?

Naive early 1900's picture:

High T



Low T

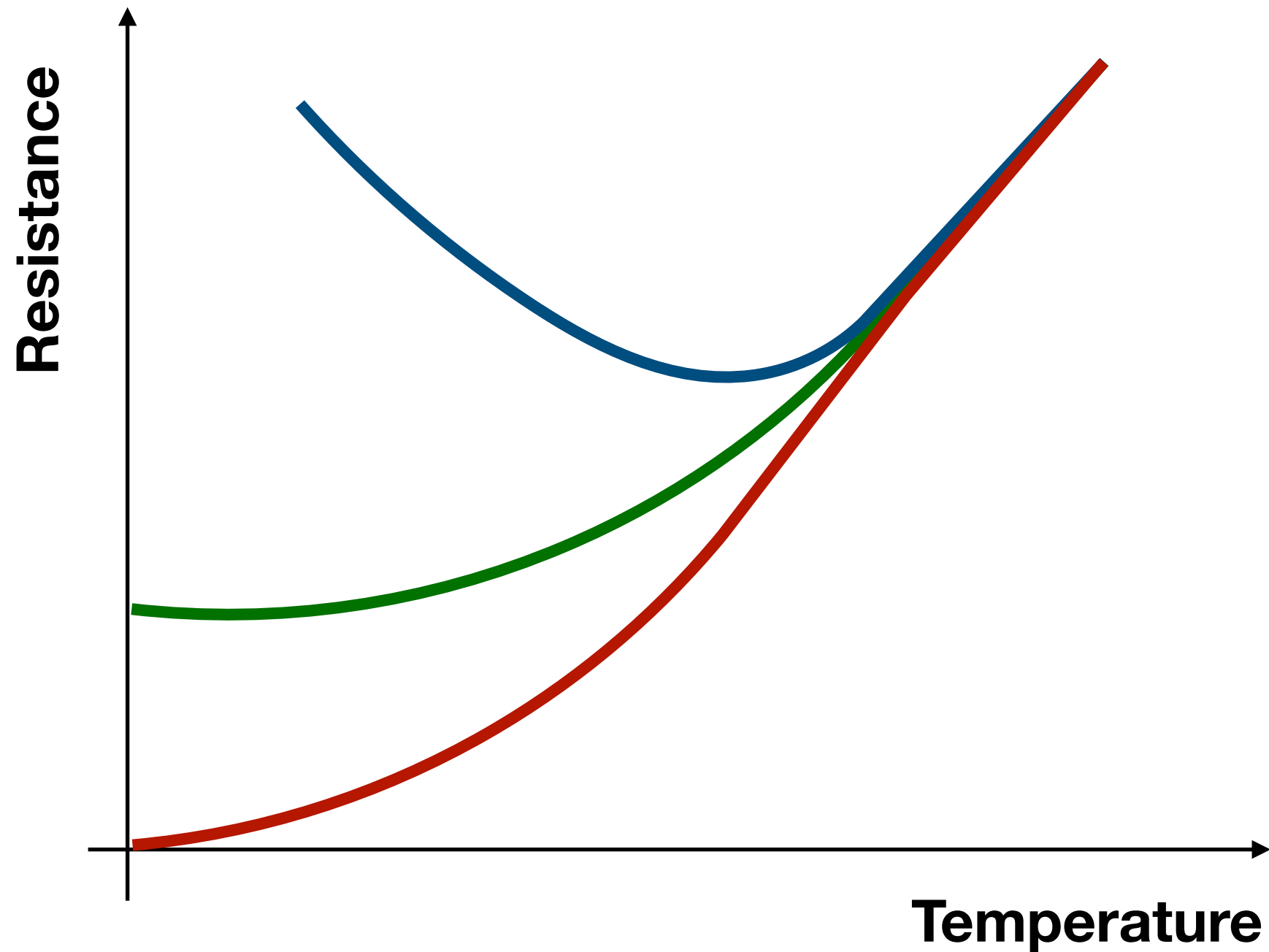


 Ion

 Electron

Q: What happens to the resistance of metals at low temperatures?

**Q: How do metals behave at low T?**

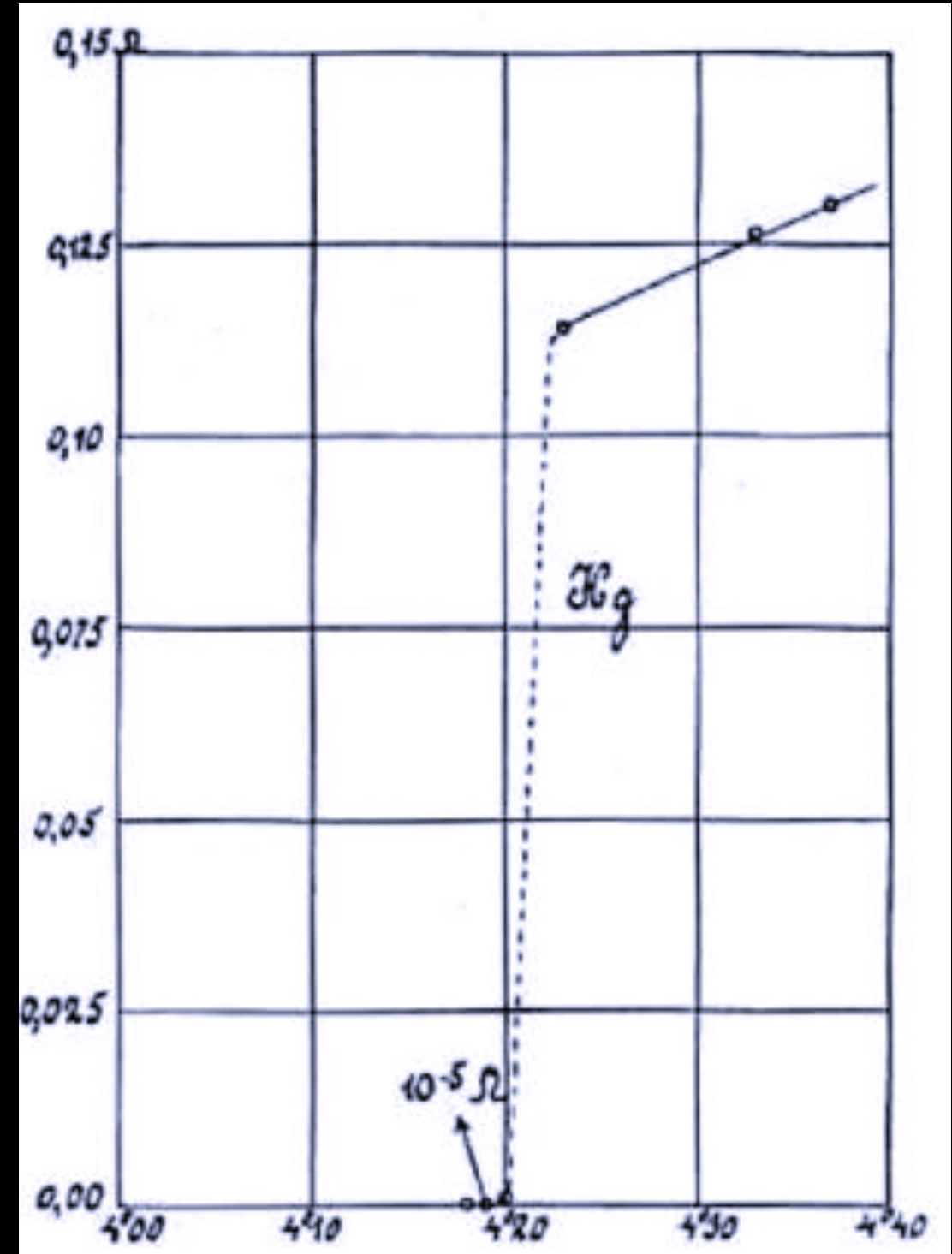




# Kamerlingh Onnes (1911)



Resistance( $\Omega$ )



Temperature (K)

**Let's first describe metals...**



**Q: Are Superconductors simply perfect conductors?**

# London Equations



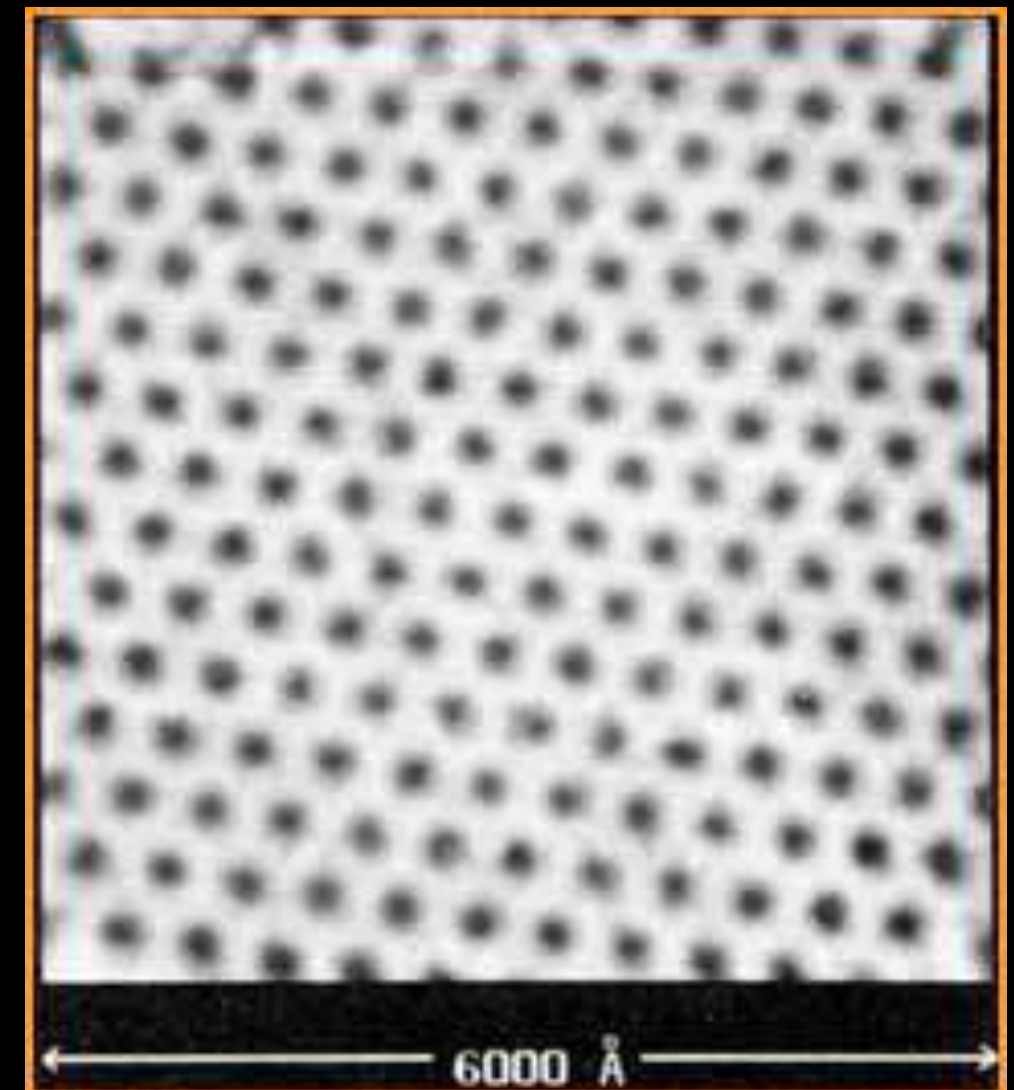
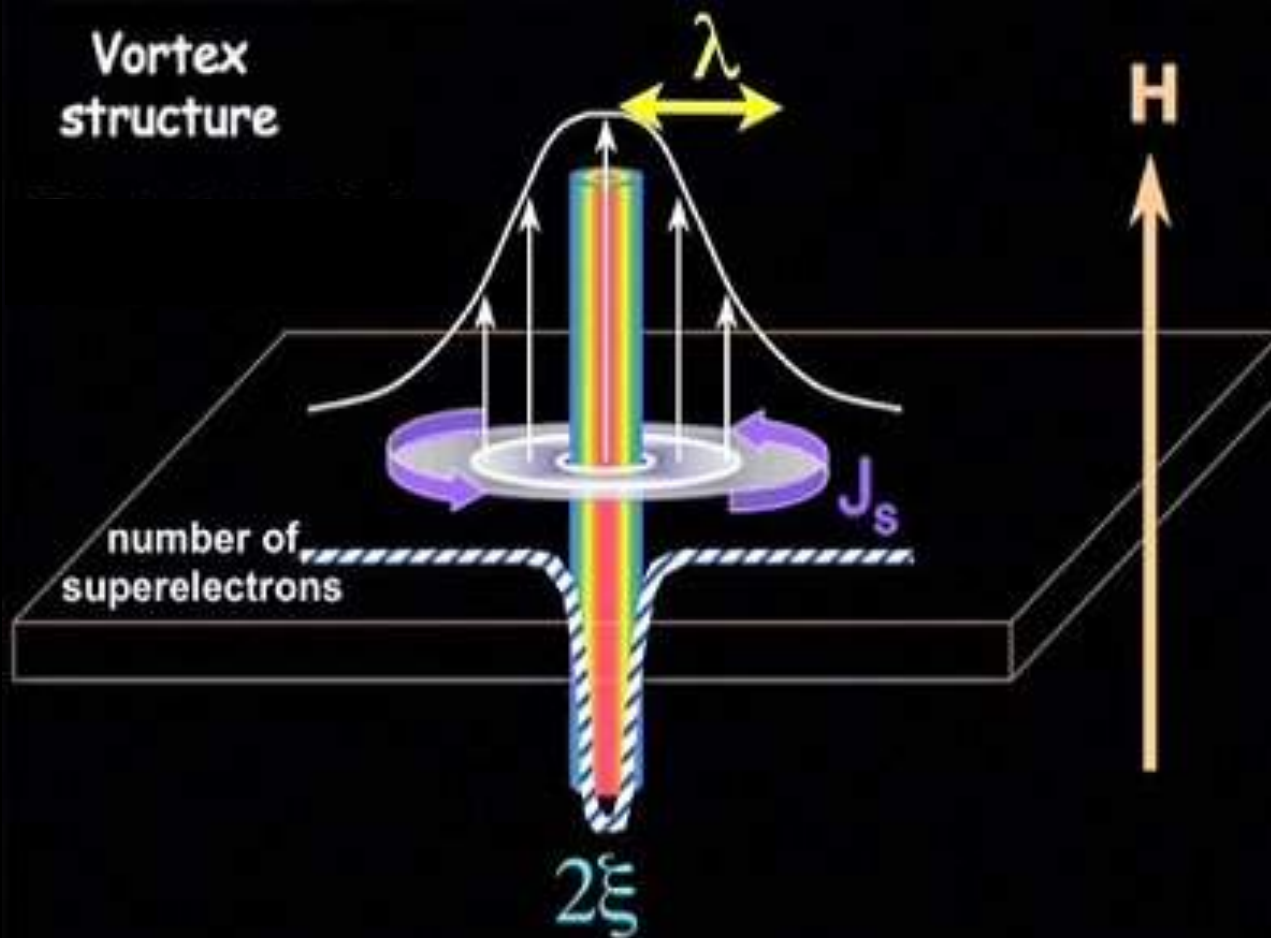
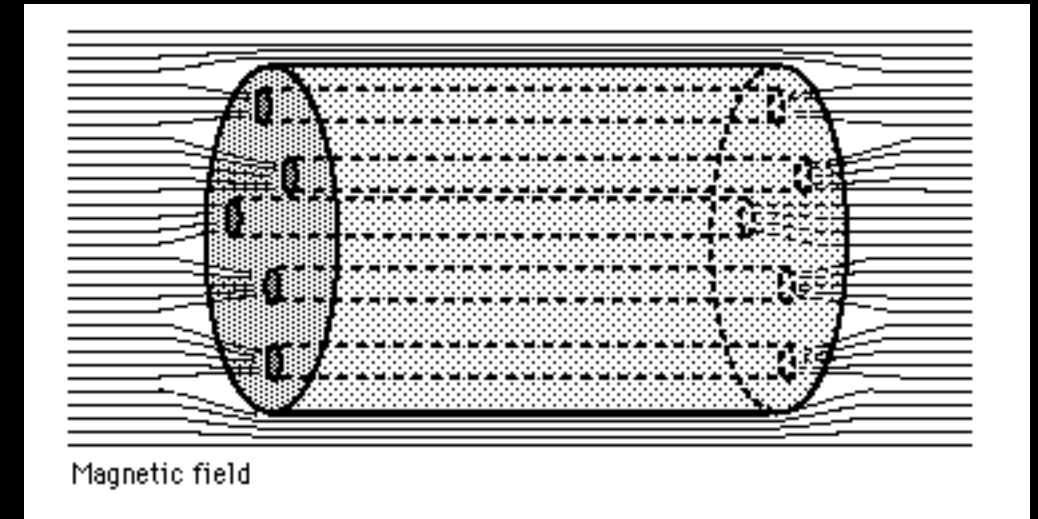
# Landau Theory of Phase Transitions

# Ginzburg-Landau Theory



# Ginzburg-Landau Theory + B

# Vortices



# Josephson Effect

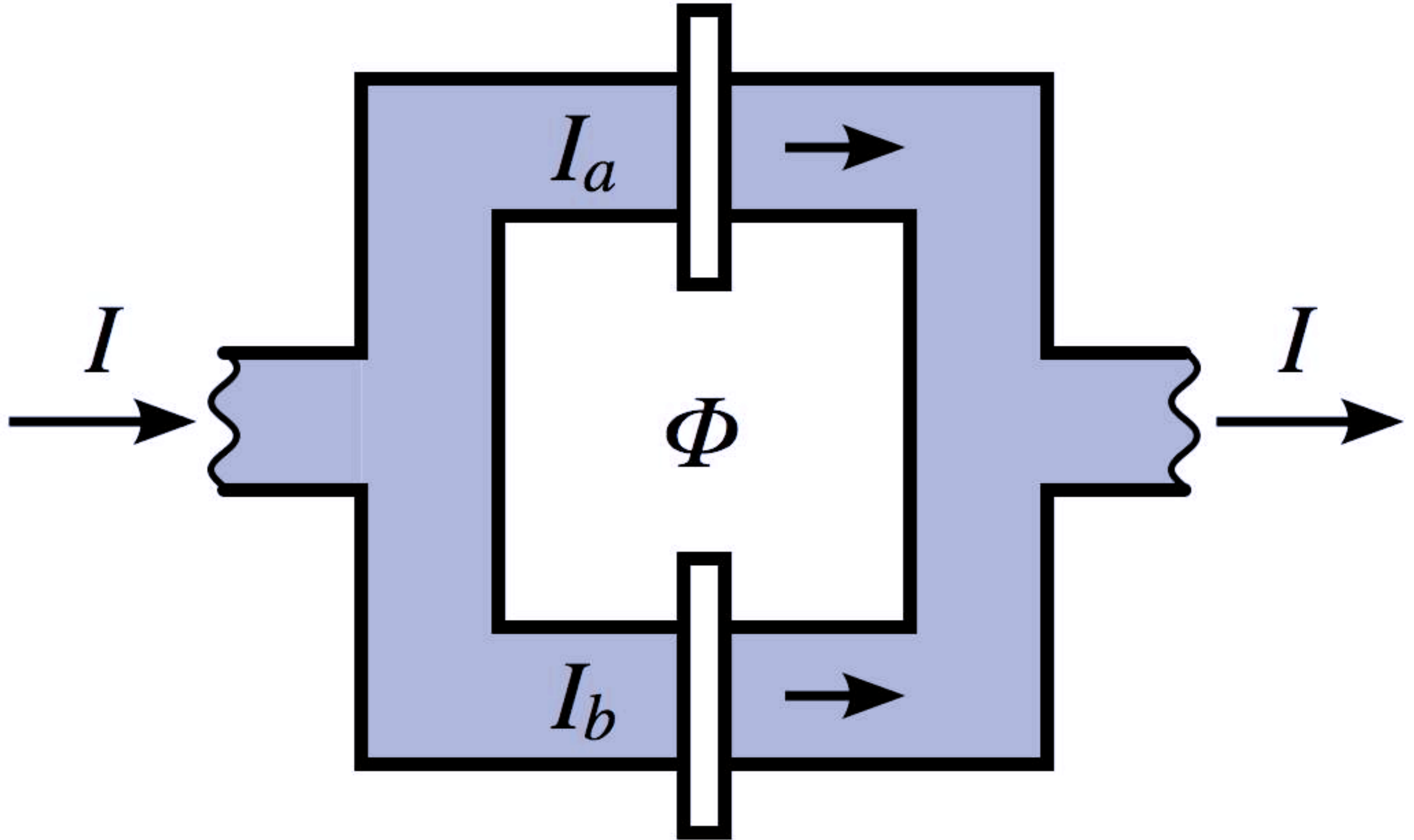


**SQUIDS**

**Fun fact: That is what you get if you google SQUID**



# SQUID: Superconducting Quantum Interference Device





# **Superconducting Q-bits**

# Some references:

**N. W. Aschcroft and N. D. Mermin, Solid State Physics, Chapters 1 (Drude), 2 (Sommerfeld), and 34 (SC)**

**C. Kittel, Introduction to Solid State Physics, Chapter 12 (SC)**

**C. P. Poole, Superconductivity, Chapters 1 and 2 (Intro), 5 (GL), 6 (\*BCS), 13.7 onwards (JJ) (note that the chapter numbers change for the latest edition of the book)**

**R. Feynman, Lecture Notes on Physics, Lecture 21: A Seminar on Superconductivity**

**P. Coleman, Introduction to Many-Body Physics, Chapters 11 (GL), 14 (\*BCS)**

## **Lecture videos:**

**S. Kivelson: Superconductivity and Quantum Mechanics at the Macro-Scale  
(<https://www.youtube.com/watch?v=Yx666k2XH8E>)**

**A. J. Millis: Microscopic Theory of SC (first 17 minutes for intro)  
(<https://boulderschool.yale.edu/2014/boulder-school-2014-lecture-notes>)**

# Further reading:

**John M. Martinis, Kevin Osborne, Superconducting Qubits and the Physics of Josephson Junctions, Les Houches School Proceedings (<https://arxiv.org/abs/cond-mat/0402415>)**

**Jaw-Shen Tsai, Toward a superconducting quantum computer: Harnessing macroscopic quantum coherence, Proc Jpn Acad Ser B Phys Biol Sci. 2010 Apr; 86(4): 275–292 (<https://www.ncbi.nlm.nih.gov/pmc/articles/PMC3417795/>)**

**G. Wendin and V. S. Shumeiko, Quantum bits with Josephson junctions (Review Article), Low Temperature Physics 33, 724 (2007) (<https://aip.scitation.org/doi/full/10.1063/1.2780165>)**

## Lecture videos:

**A. Blais: Quantum Computing with Superconducting Qubits (Part 1) - CSSQI 2012 ([https://www.google.com/url?hl=en&q=https://www.youtube.com/watch?v%3Dt5nxusm\\_Umk&source=gmail&ust=1532610408235000&usg=AFQjCNGYRSGU5EFyFPSfOZGalGFdRhOfkQ](https://www.google.com/url?hl=en&q=https://www.youtube.com/watch?v%3Dt5nxusm_Umk&source=gmail&ust=1532610408235000&usg=AFQjCNGYRSGU5EFyFPSfOZGalGFdRhOfkQ))**

**The first part of this video gives a good idea of how Josephson Junctions are important for SC-circuit based Q-Bits.**